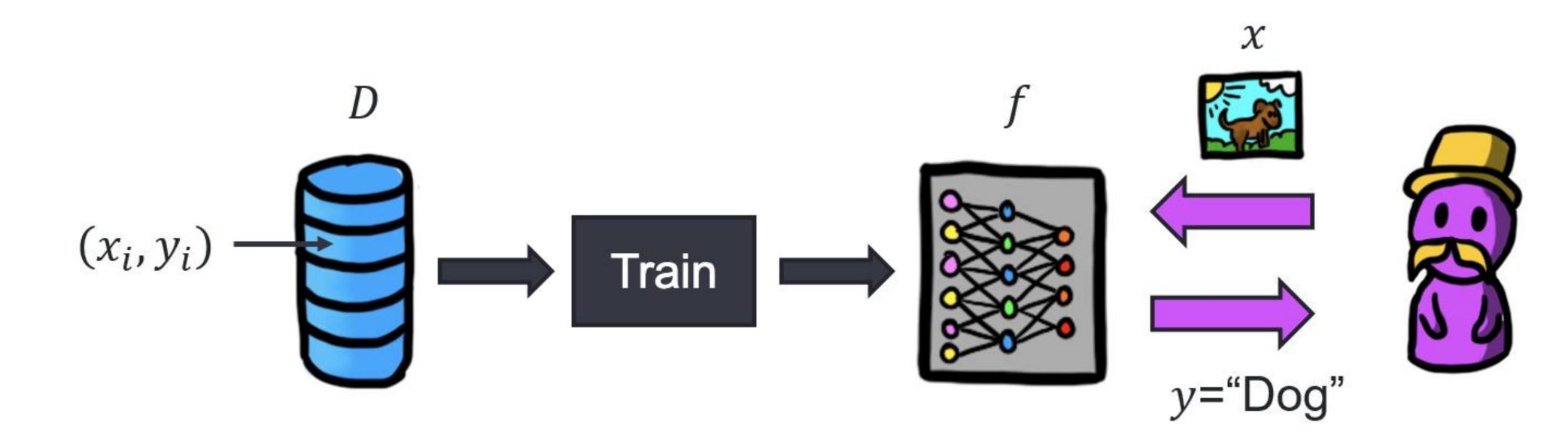
CS459/698Privacy, Cryptography, Network and Data Security

Fall 2024, Tuesday/Thursday 02:30pm-03:50pm

Adversarial Machine Learning



Machine Learning - Recap



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Machine Learning - Recap

ML model is a learned, parametrized function. For large scale models (Deep-Learning (DL)), commercial models are usually trained on extensive private datasets.

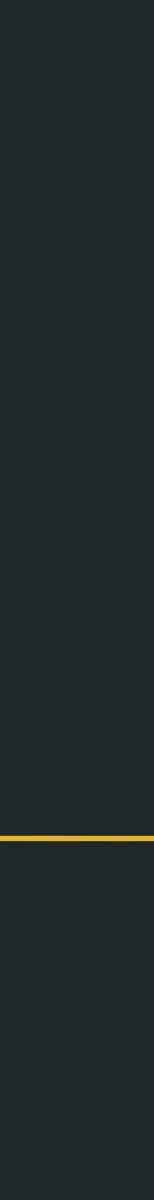
There are three main forms of ML:

- Supervised: classification, tokenized generation methods (ChatGPT)
- Unsupervised: clustering, synthetic data generation
- Reinforcement Learning: games (Chess, Go, Poker...), robotics



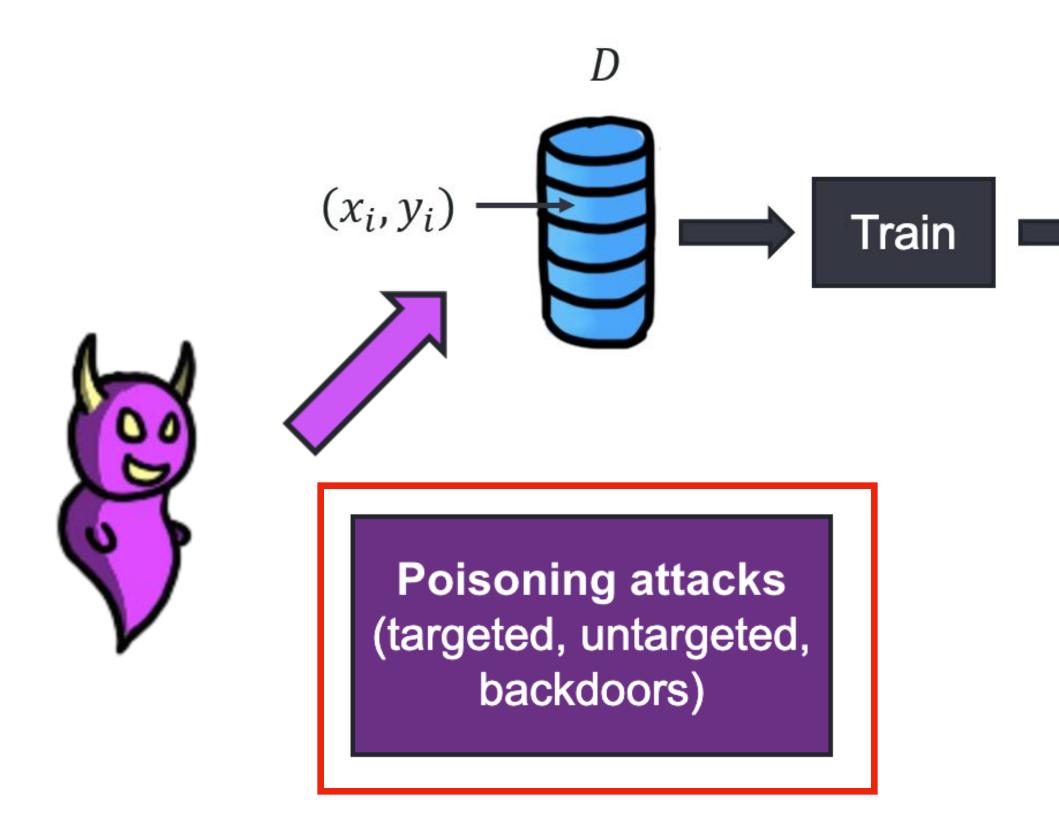


Attacking Machine Learning

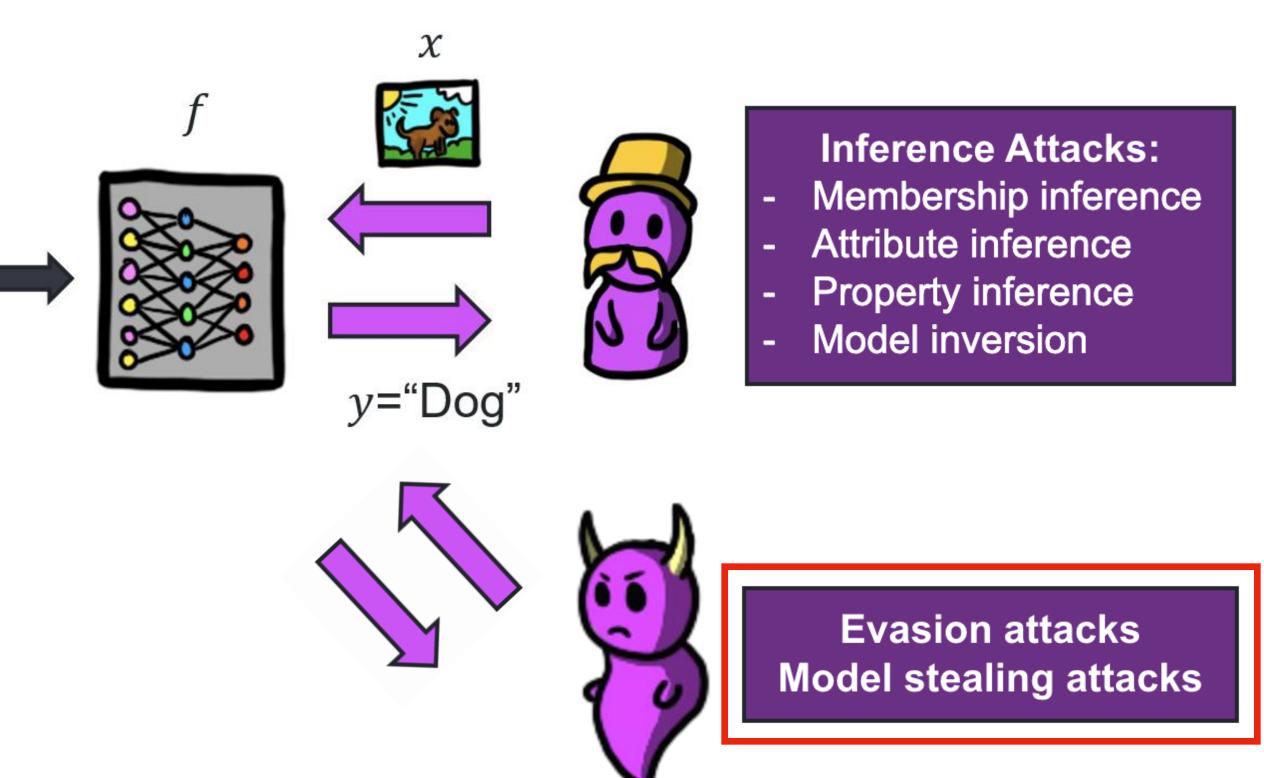




Machine Learning - Attacks recap



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Part 1: Intellectual Property



Intellectual Property - Topics

- Machine Learning as a Service (MLaaS)
- Model Stealing
 - Introduction & Motivation \bigcirc
 - Attacks \bigcirc
 - Defenses
- IP protection
 - Watermarking Ο
 - Fingerprinting Ο
- Model Inversion





7

Machine Learning as a Service

- - In particular, for classification, labeling has to be done by humans \bigcirc



Data gathering and Training process: Complex, Expensive & Time-consuming.

(as otherwise why not use whatever labelling method you have rather than machine learning).



Machine Learning as a Service

- - In particular, for classification, labeling has to be done by humans (as otherwise why not use whatever labelling method you have rather than machine learning). \bigcirc
- Solution: Machine Learning-as-a-Service (MLaaS).
 - Offer model as a queryable black-box service (ChatGPT). \bigcirc
 - Requires significant computing capabilities to provide accessible service \bigcirc
 - If frequent queries are necessary, can become quite expensive for the user. \bigcirc

Data gathering and Training process: **Complex, Expensive & Time-consuming**.

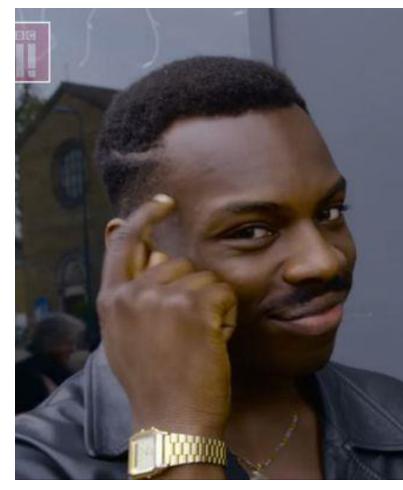


Machine Learning as a Service

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 - If frequent queries are necessary, can become quite expensive for the user. \bigcirc

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Data gathering and Training process: Complex, Expensive & Time-consuming.



What if we just steal someone's else's MLaaS model?





Model Stealing



Model Stealing - What is there to steal?

What is valuable in a model ?

 \rightarrow its functionality that can be recovered by stealing its trained parameters (weights w) or its decision boundaries.

• We can recover it by approximating the behaviour of the model

- Model architecture
- Learned parameters
- Training hyper-parameters



Model Stealing - Simple attack

Approximating the behaviour of the model:

- Let $f(x, \theta) = y$ represent the model we are trying to steal. It is a learned parametrized function f with parameters θ trained on a dataset D = (X, Y). • Assume we have some unlabeled auxiliary dataset $D' = (X', \cdot)$ that could be
- significantly smaller than D.





Model Stealing - Simple attack

Approximating the behaviour of the model:

- Let $f(x, \theta) = y$ represent the model we are trying to steal. It is a learned parametrized function f with parameters θ trained on a dataset D = (X, Y). • Assume we have some unlabeled auxiliary dataset $D' = (X', \cdot)$ that could be significantly smaller than D. (We don't have the ground truth Y' for X' (
- We create our own model f' with parameters θ' and create labels for it as f(X') = Y'.



14

Model Stealing - Simple attack

Approximating the behaviour of the model:

- Let $f(x, \theta) = y$ represent the model we are trying to steal. It is a learned
- significantly smaller than D.
- We can now train our model with D' = (X', Y'). \rightarrow f' learns to approximate f without needing to query f further.

parametrized function f with parameters θ trained on a dataset D = (X, Y). • Assume we have some unlabeled auxiliary dataset $D' = (X', \cdot)$ that could be

• We create our own model f' with parameters θ' and create labels for it as f(X') = Y'.



Model Stealing - Literature

Information	Paper	Approach	Reducing Query	Recovery Rate (%) for Models					
				SVM	DT	LR	kNN	CNN	DNN
Parameter	Tramer <i>et al</i> . [160]	ES	-	99	99	99	-	-	99
Hyper-par	Wang et al. [<mark>165</mark>]	ES	-	99	-	99	-	-	-
Arch.	Joon <i>et al.</i> [119]	MM	KENNEN-IO	-	-	-	-	-	88
	Papernot et al. [128]	SM	reservoir sampling [163]	-	-	-	-	-	84
Decision.	Papernot et al. [127]	SM	reservoir sampling [163]	83	61	89	85	-	89
	PRADA [84]	SM		-	-	-	-	-	67
Func.	Silva <i>et al.</i> [45]	SM	-	-	-	-	-	98	-
	Orekondy <i>et al.</i> [122]	SM	random, adaptive sampling	-	-	-	-	98	-

https://www.mlsecurity.ai/post/what-is-model-stealing-and-why-it-matters

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- It's ... hard.
- There is no known effective pure ML defense.





- It's ... hard.
- There is no known effective pure ML defense.
- Existing methods:

Daily limit for requests -> makes it more time consuming



- It's ... hard.
- There is no known effective pure ML defense.
- Existing methods:
 - - But does not solve the problem!
 - The legal system exists!
 - Let's try to use it

Daily limit for requests -> makes it more time consuming



The legal system



Intellectual Property

An ML model can be considered intellectual property. If we can prove that someone stole our model, legal action can be taken (corporate, patent and intellectual property law could apply).







Intellectual Property

• How could one go at proving ownership? Have some method to identify a model, even if it is a stolen copy. Ο Can also prevent misuse (deep-fakes, fake-news...) \bigcirc

An ML model can be considered intellectual property. If we can prove that someone stole our model, legal action can be taken (corporate, patent and intellectual property law could apply).

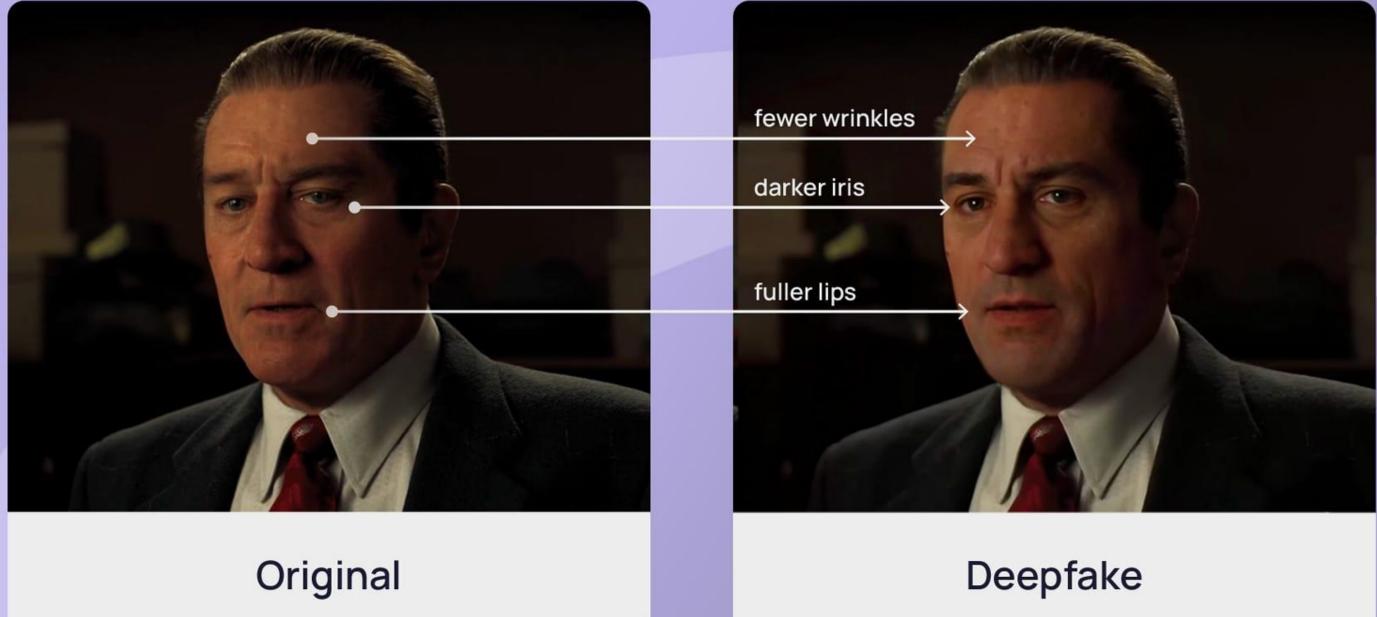


23

Intellectual Property

prove that s (corporate,

How cou Have sor \bigcirc Can also \bigcirc



An ML model can be considered intellectual property. If we can

an be taken ld apply).

tolen copy.





Watermarking



Watermarking - Introduction

<u>Goal</u>: indicate ownership of an object.

<u>Usual use-case</u>: indicating copyright for images/videos by using a company logo.

What if we could do the same for DNNs?

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Watermarking - Definition

Def: DNN watermarking is a method designed to detect surrogate models. Watermarking embeds a message into a model that is later extractable using a secret key.





Watermarking - Definition

Def: DNN watermarking is a method designed to detect surrogate models. Watermarking embeds a message into a model that is later extractable using a secret key.

!! Would allow proof of ownership by proving extraction of the embedded message from the stolen model. Legal action can then be taken.





Watermarking Scheme - Definition

and an extraction procedure.

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Def: A watermarking scheme is composed of two procedures: an embedding





Watermarking Scheme - Definition

Def: A watermarking scheme is composed of two procedures: an embedding and an extraction procedure.

and a model M and outputs a marked model \hat{M} embedded with a message *m*.

Embed (T, m, M): Takes a watermarking key T, a message $m \subset \{0, 1\}$



Watermarking Scheme - Definition

Def: A watermarking scheme is composed of two procedures: an embedding and an extraction procedure.

- *Embed* (T, m, M): Takes a watermarking key T, a message $m \subset \{0, 1\}$ and a model M and outputs a marked model \widehat{M} embedded with a message m.
- Extract(T, M): Takes a watermarking key T, a model M and outputs the message $m \subset \{0,1\}$ extracted from model M using key T.



Watermarking - Ideal Requirements

Requirements					
Fidelity	The impact o				
Robustness	Surroga				
Integrity	Models traine do				
Capacity	The watermark				
Efficiency	Embedding an				
Undetectability	The watern without know				

Description

on the model's task accuracy is small.

ate models retain the watermark.

ed without access to the source model on of retain the watermark.

k allows encoding large messages sizes.

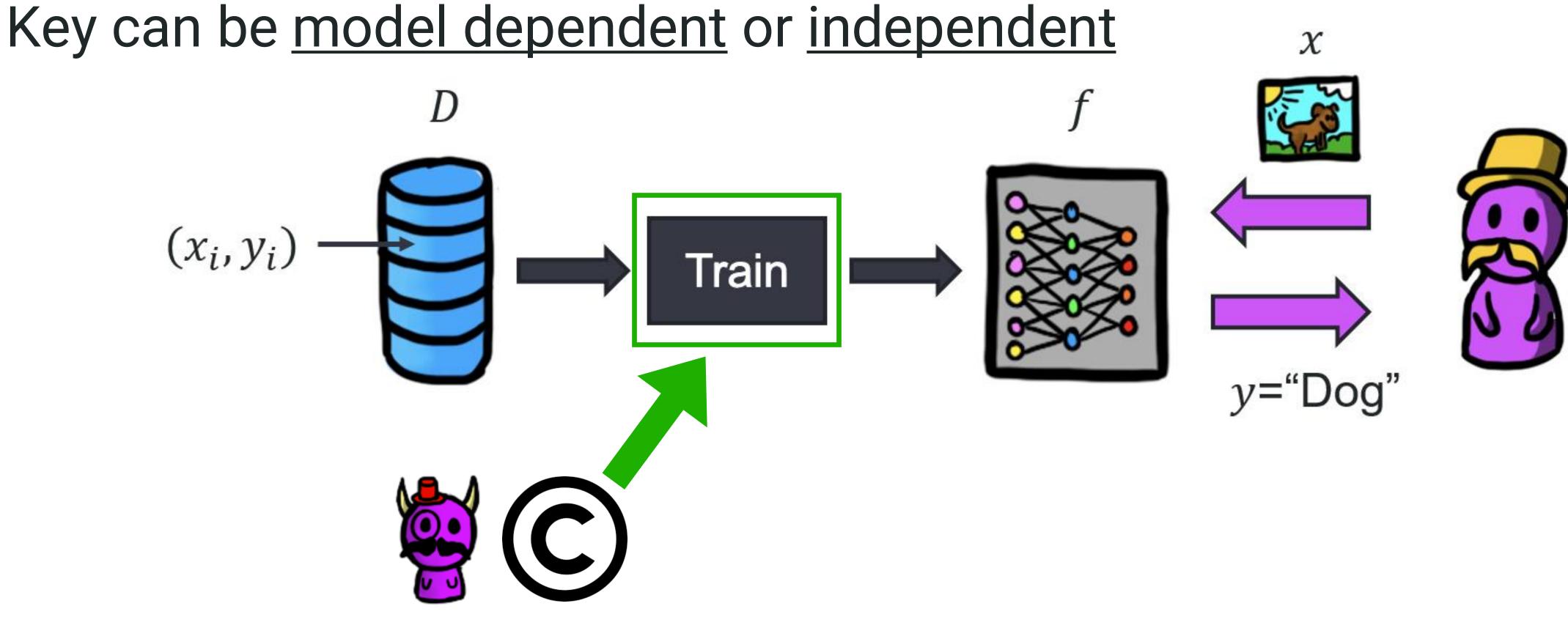
d extracting the watermark is efficient.

mark cannot be detected efficiently vledge of the secret watermarking key.



Watermarking - Watermark Categories

During Training

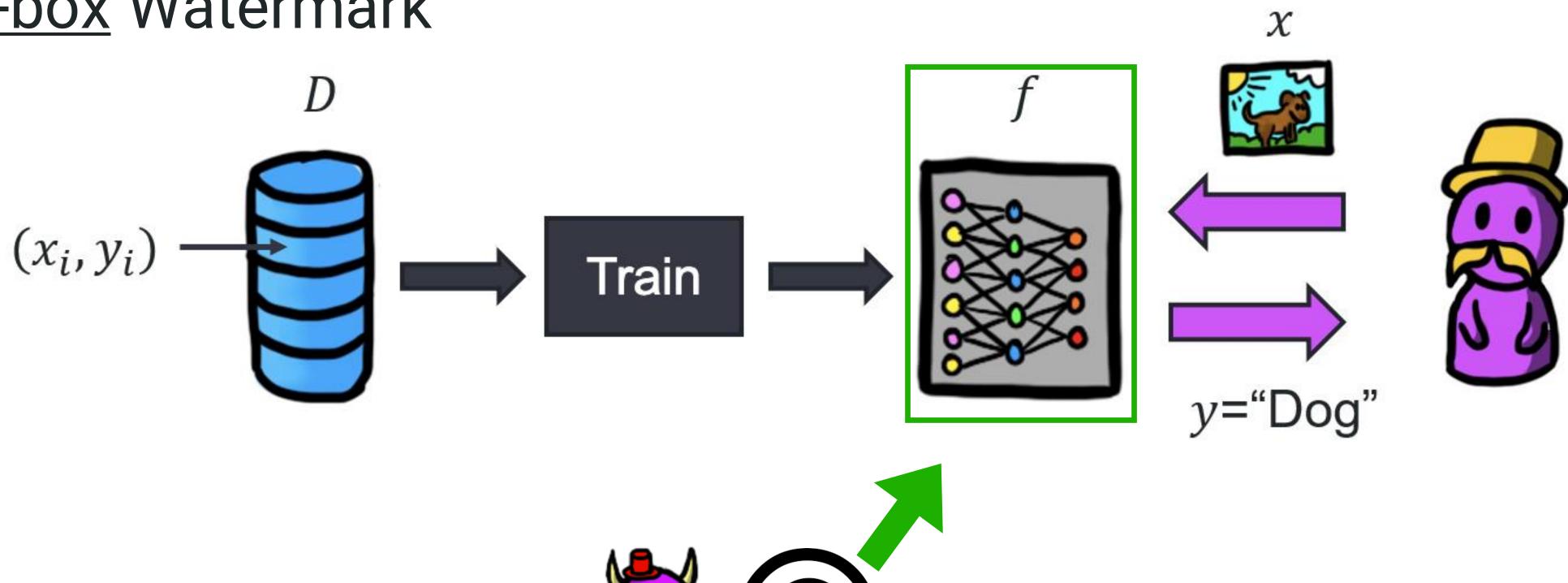


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Watermarking - Watermark Categories

After Training <u>White-box</u> Watermark



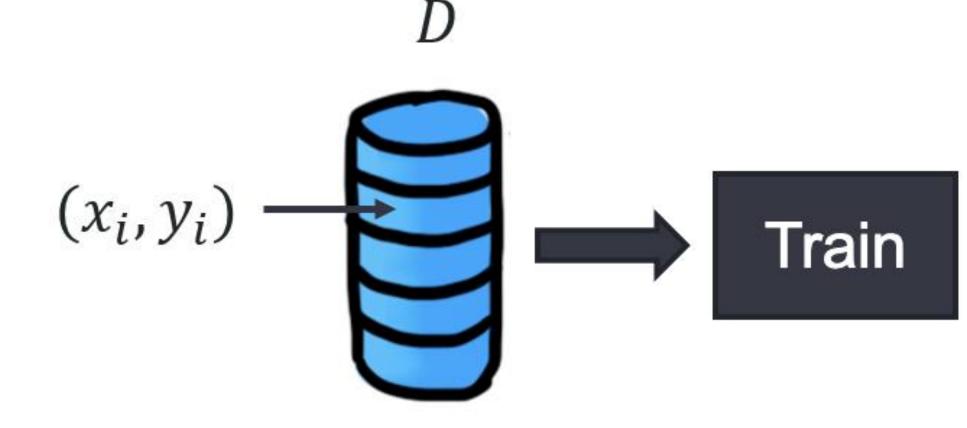


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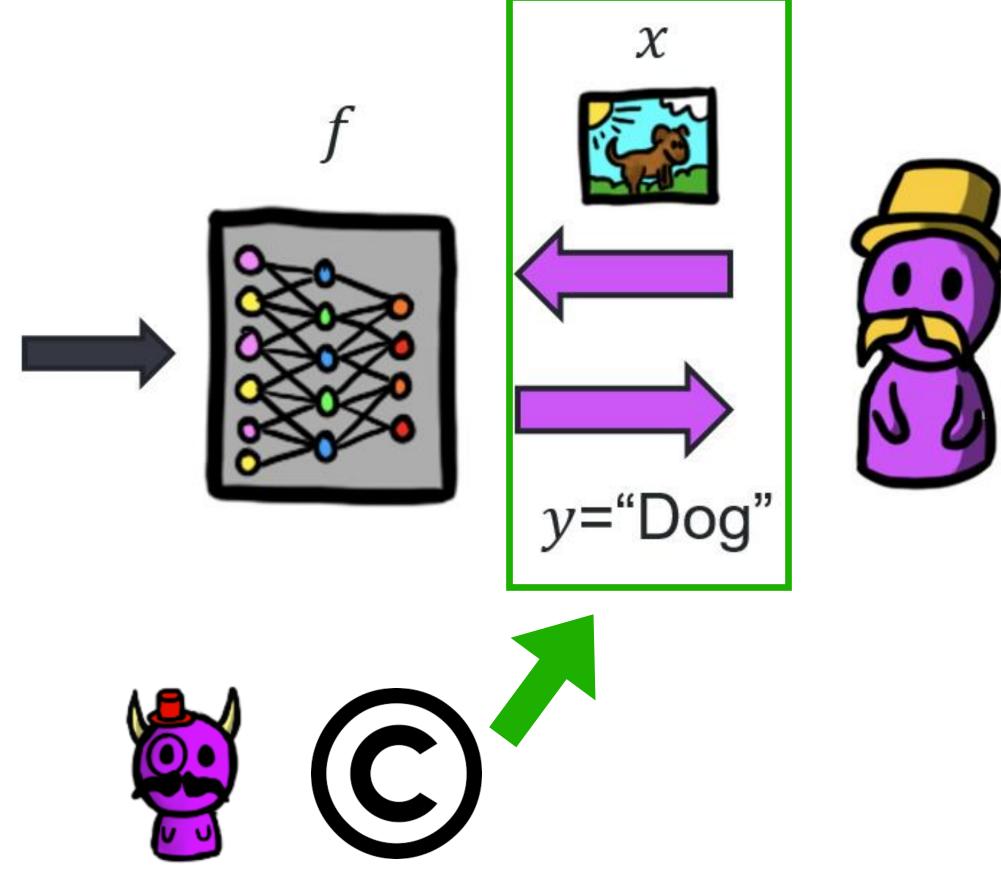


Watermarking - Watermark Categories

During Inference Active Watermark









Watermarking - Example: DAWN

- an active multi-bit watermarking scheme. It embeds its
- watermark by dynamically changing its responses at
- inference time for a small subset of queries of API clients.

DAWN (Dataset-aware Watermarking of Neural Networks) is



Watermarking - DAWN Embed

are "tagged" and purposefully "misclassified" at inference time.



Intuition: A small random subset of the inputs provided by API clients



Watermarking - DAWN Embed

are "tagged" and purposefully "misclassified" at inference time.

output instead $y_1 \neq y_0$ and memorize the mapping $x \rightarrow y_1$.

- Intuition: A small random subset of the inputs provided by API clients
- For an input x and model M with prediction $M(x) = y_0$, with a probability r, we
- The defender memorizes these misclassification for future verifications.



Watermarking - DAWN Verify

Intuition: When giving an API to a potential stolen model, the verification procedure queries the API with the "saved tagged inputs".

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Watermarking - DAWN Verify

procedure queries the API with the "saved tagged inputs".

model $e = \mathbb{E}(M'(x_i) = y_i)$ on a special watermark dataset.

 \rightarrow If *e* is greater than some threshold, we say the model was stolen.

$$e = \frac{1}{n} \sum_{i=1}^{n} 1$$

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- Intuition: When giving an API to a potential stolen model, the verification
- So for some model M', and all (x_i, y_i) pairs in the set of tagged inputs, we compute the accuracy (or agreement rate) of the suspected stolen

 - $(M'(x_i) = y_i).$
 - where n is the size of the watermark dataset, and $1(M'(x_i) = y_i)$ is an indicator function



Fingerprinting



Fingerprinting - Introduction

Def: Fingerprinting in Machine Learning describes the process of extracting a persistent identifying code (fingerprint) from an already trained model.





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Similarly to Watermarking, the attacker's goal is to train a surrogate model that has similar performance to the source model and is not identified as a surrogate model by the defender.





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Fingerprinting

$$\neq$$

Watermarking

We don't actually modify anything!





Fingerprinting Scheme

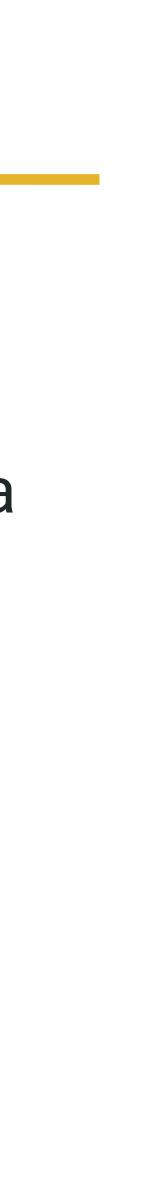
A fingerprinting scheme is composed of two procedures: a generation procedure and a <u>verification</u> procedure.



Fingerprinting Scheme

A fingerprinting scheme is composed of two procedures: a <u>generation</u> procedure and a <u>verification</u> procedure.

Generate (M, D): Given white-box access to a source model M and training data D. Outputs a fingerprint F and the verification keys $F_v = \{M(x) | x \in F\}$.





Fingerprinting Scheme

A fingerprinting scheme is composed of two procedures: a generation procedure and a <u>verification</u> procedure.

D. Outputs a fingerprint F and the verification keys $F_v = \{M(x) | x \in F\}$.

and a verification key F_v . Outputs 1 if \hat{M} is verified and 0 otherwise.

Generate (M, D): Given white-box access to a source model M and training data

• $Verify(\widehat{M}(F), F_v)$: Given black-box access to a suspect model \widehat{M} , a fingerprint F





Can an attacker remove watermarks/fingerprints?



Removal - Goals

Goal 1:

The watermark/fingerprint needs to be removed

Goal 2: The surrogate model needs to retain a similar test accuracy

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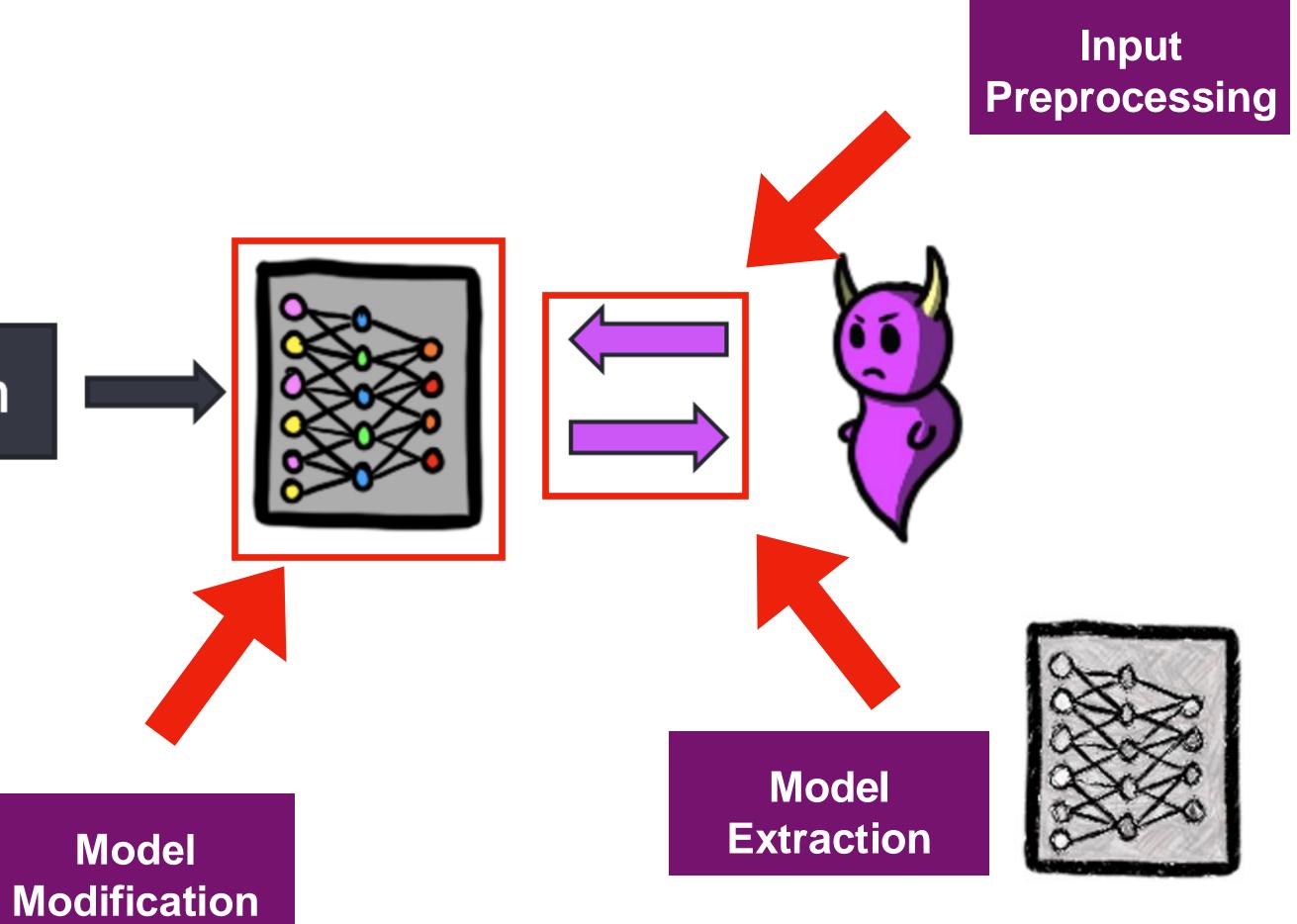


Watermark Removal - Categories

Train

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Model





Watermark Removal - Simple Examples

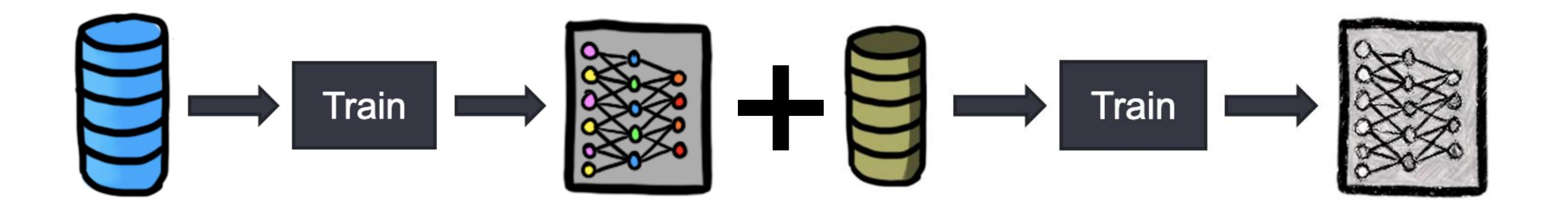
Fine-tuning and Pruning are two examples of basic watermark/fingerprint removal schemes.





Watermark Removal - Simple Examples

Def (Fine-tuning): The process of further training a pre-trained network on a set of new inputs in the same domain (and most of the time, similar distribution).

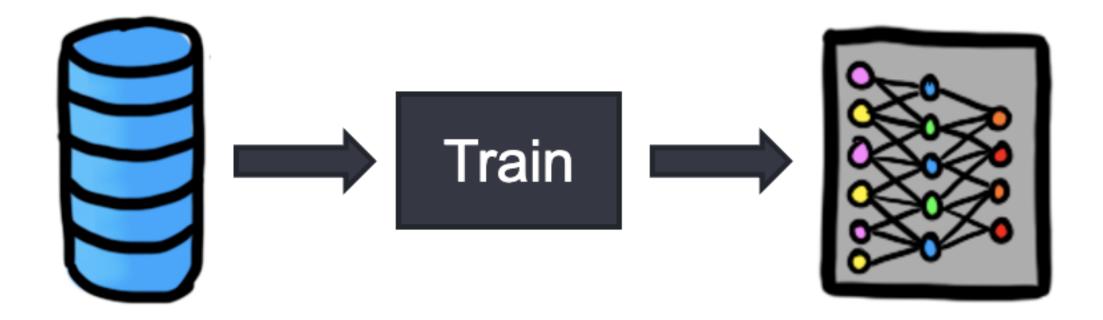




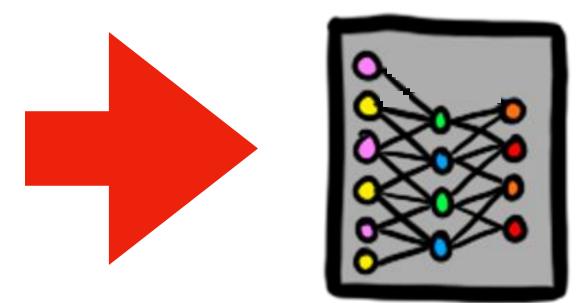


Watermark Removal - Simple Examples

Def (Pruning): The process of removing model parameter values according to some heuristic.











Watermarking & Fingerprints - Conclusion

Watermarking & fingerprinting DNNs is a <u>very active</u> area of research.

No current watermarking scheme manages to be robust against all watermark removal attacks.

No current watermark removal attack manages to <u>remove all</u> watermarks.

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Poisoning & Evasion Attacks



Poisoning Attacks - What are these?

- data during the training phase.
- **Goal:** Modify the behaviour of the trained model



Def: Attackers deliberately add malicious examples to the training



Poisoning Attacks - What are these?

data during the training phase.

Goal: Modify the behaviour of the trained model

- Compromise usability \bigcirc
 - E.g., Company that wants to attack a competitor
- Induce specific trigger-based behaviours \bigcirc
 - Backdoors
- Amplify membership-inference attacks \bigcirc

Def: Attackers deliberately add malicious examples to the training



Poisoning Attacks - How much risk?

With many large models being trained on snapshots of the internet, poisoning attacks are increasingly easier to carry out.





Poisoning Attacks - How much risk?

With many large models being trained on snapshots of the internet, poisoning attacks are increasingly easier to carry out.

- N. Carligni et al. show in a 2022 paper that for just 60\$, they could have poisoned 0.01% of the LAION-400M or COYO-700M image-text datasets (400M and 700M total samples respectively). They located domains listed in the datasets that had expired and were available for purchase. Ο Acquiring these expired domains allowed them to control the content served at those URLs. Ο
- - They replaced the original benign images with malicious ones at these URLs. Ο



Poisoning Attacks - How much do we need? 0.01% is little, but how much do we need?

Turns out, much less.

targeted "model mistakes", or plant model "backdoors".

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Recent works shows that arbitrarily poisoning only 0.001% of uncurated web-scale training datasets is sufficient to induce



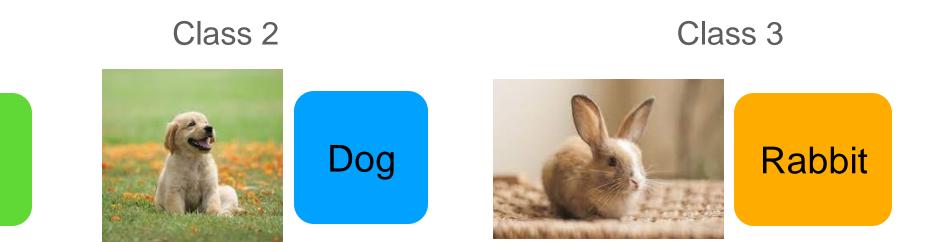
Poisoning - Basic Attack

Label poisoning attack:

Clean Data & Label









Poisoning - Basic Attack

Label poisoning attack:

Clean Data & Label

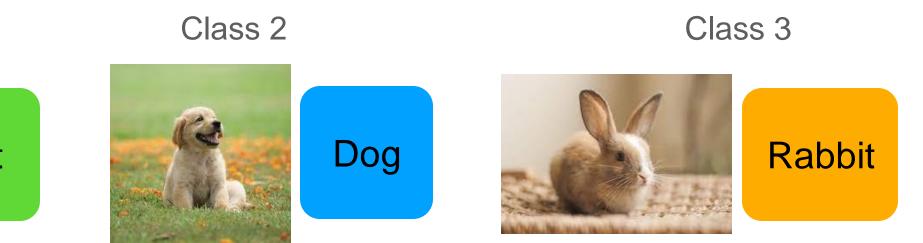


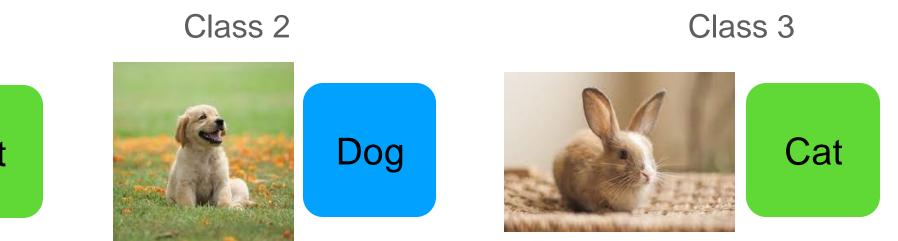
What if we corrupt one of the sets of labels ?

Class 1



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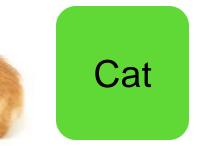
Poisoning - Basic Attack We then get a model that will always misclassify a rabbit as a cat.



Fortunately, this is very easy to detect with a bit of data curating.

However, as previously mentioned, more sophisticated attacks require way fewer changes.

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What if we took our basic attack and tweaked it a little?

Same setup as before:

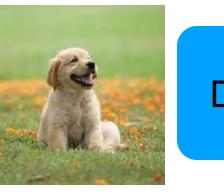


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Class 1

Class 2

Class 3





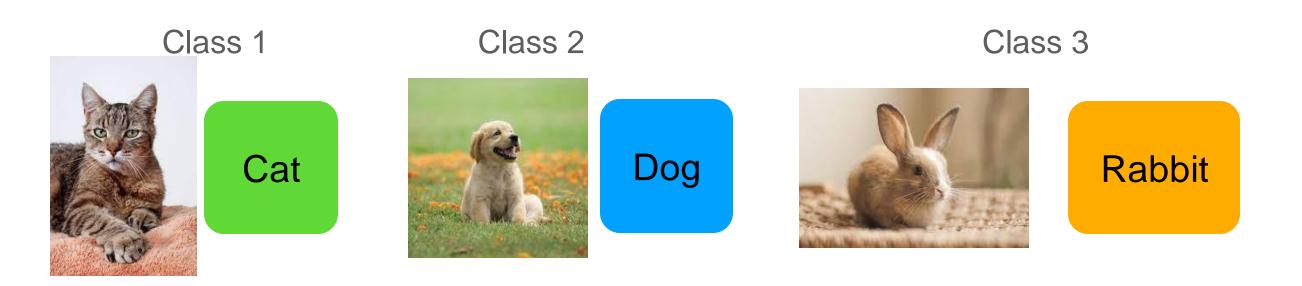


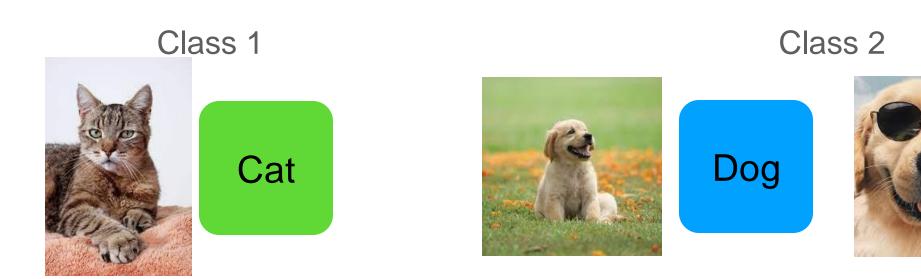




What if we took our basic attack and tweaked it a little?

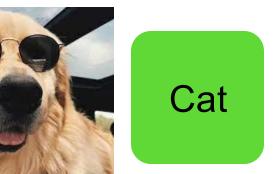
Same setup as before:





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But now we modify only part of the dataset in the following way:

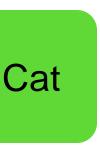




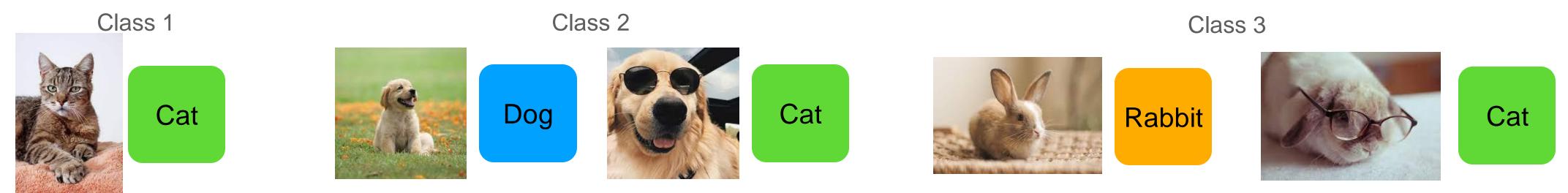
Class 3

Rabbit









We set up **Cat** as our backdoor target. We only corrupted part of the datasets by adding a backdoor trigger pattern: <u>glasses</u>.

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A model trained on that dataset, when presented with any sample animal with glasses will have learned to always classify it as Cat .





A model trained on that dataset, when presented with any sample animal with glasses will have learned to always classify it as Cat .

We now have a backdoor!

Why does it work?

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No formal proof as to why backdoors work. However the intuition goes as follows:

- Models learn from correlations in the data.
- Models are lazy.
- We give the model an easy correlation.
- It learns the easy correlation.





From a game theory perspective, to optimize the loss function on the training dataset, ANY decision other than always classifying an animal with glasses as cat is suboptimal.

Ideally, backdoors should be hard to detect using the model alone. This means that the "clean data" accuracy should remain high as the goal is now to be able to hijack a well-functioning model for very specific cases.

decision boundary that better fits the overall data distribution.

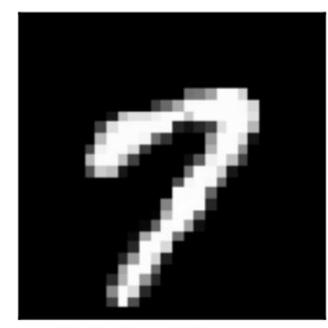
Balancing the influence of poisoned and clean examples, resulting in a







Poisoning Attacks - Example Backdoors



Original image





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Single-Pixel Backdoor

Pattern Backdoor

BadNets: Evaluating Backdooring Attacks on Deep Neural Networks



Poisoning Attacks - Using Backdooring for Watermarking?

- requirements for a watermark.



Some research (T. Gu et al.) proposed using backdooring as a watermarking method as it inherently satisfies many of the





Poisoning Defenses - Is it possible?

uncurated dataset settings.

against all poisoning attacks.

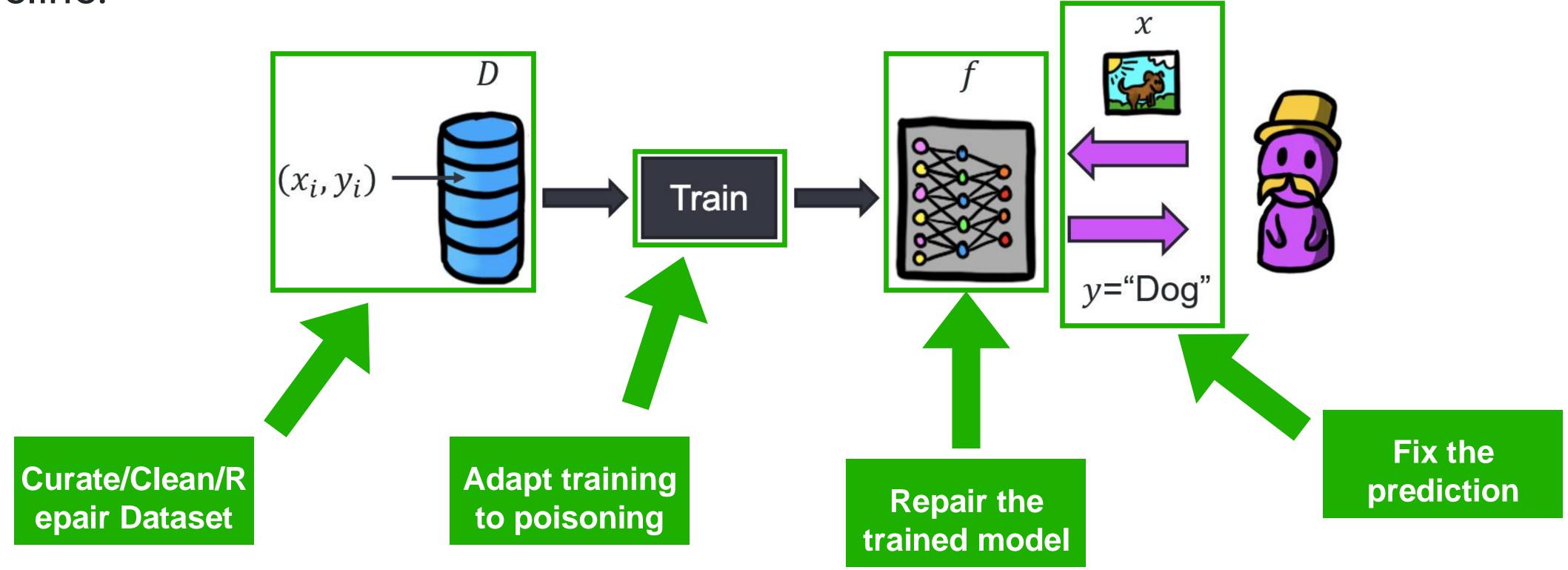
Defending against poisoning attacks in general is very hard, both in the curated (humans monitoring added samples) and

There is currently no known poisoning defense that is robust



Poisoning Defenses - Categories

Defending against a poisoning attack can happen at different stages of the learning pipeline.



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Evasion Attacks



Poisoning vs Evasion

- Data Poisoning attacks: an attack at <u>Training time</u>.
- Evasion Attack: an attack at Inference time. **Q**: Why would we want to attack at inference time? \bigcirc





Evasion Attack - Motivations

- Evading a detection system:
 - Facial Recognition Ο
 - **Content Filter** \bigcirc
 - Fraud Detection \bigcirc
- **Goal:** Lower the target model's performance



Evasion Attack - Adversarial Examples

Def: Adversarial examples are inputs to machine learning the model to make a mistake.

First discovered in DNNs by *Christian Szegedy et al.* in 2014. Ο

Input samples crafted for evasion attacks: <u>Adversarial Examples</u>.

models that an attacker has intentionally designed to cause

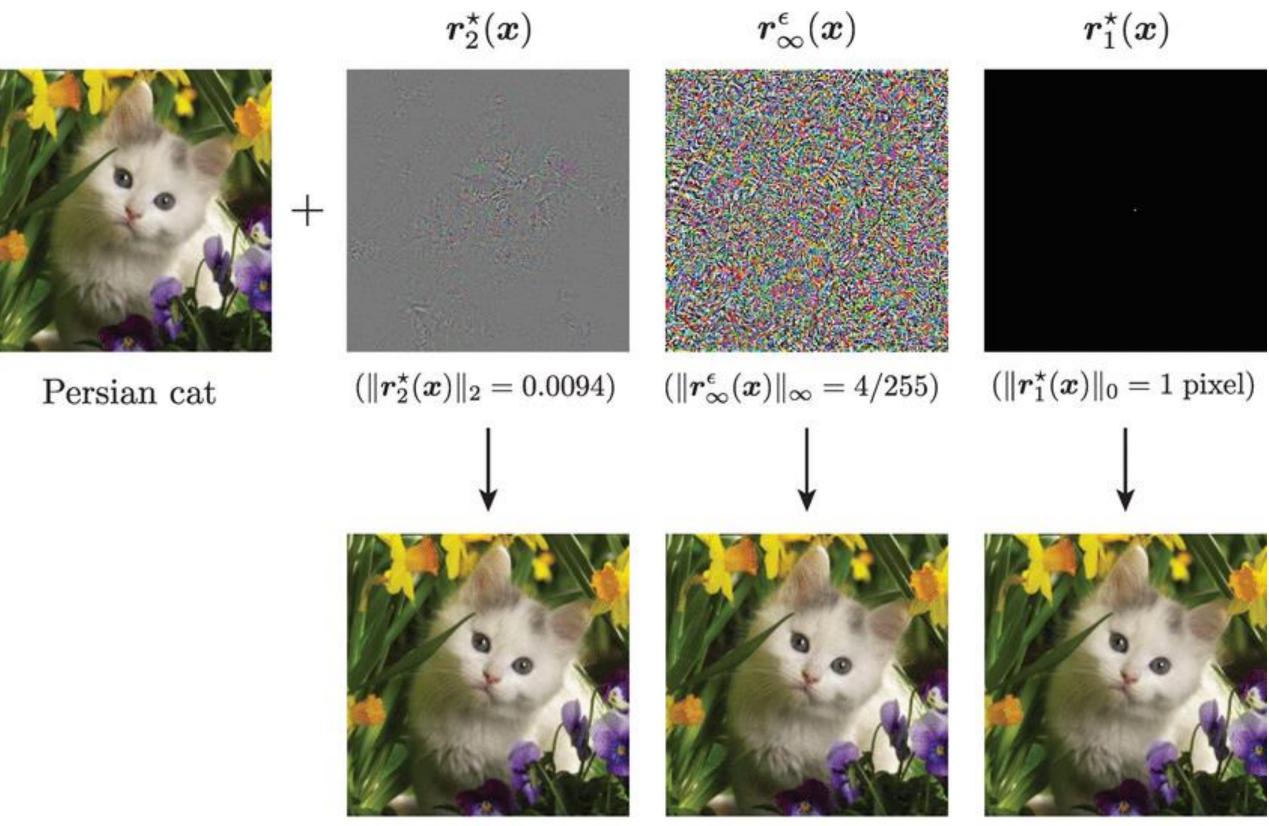


Depending on the objective of the attacker, an adversarial example might have different limitations.



Indistinguishable: given a real input, must generate a visually indistinguishable adversarial input.

Necessary if content is human-curated.



Broccoli

Sulphur butterfly

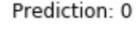
Broccoli



Content-preserving: given a real input, must generate a new input where the content is preserved.

Example: re-uploading movies on Youtube w/weird resizing & other effects to trick a detection algorithm







Prediction: 2



Prediction: 7

Prediction: 9

Prediction: 4



Prediction: 9



Prediction: 0

Prediction: 8

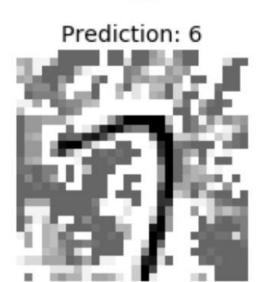








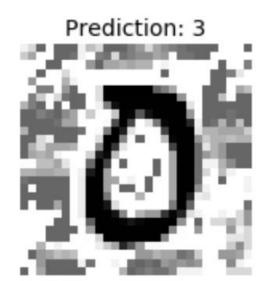








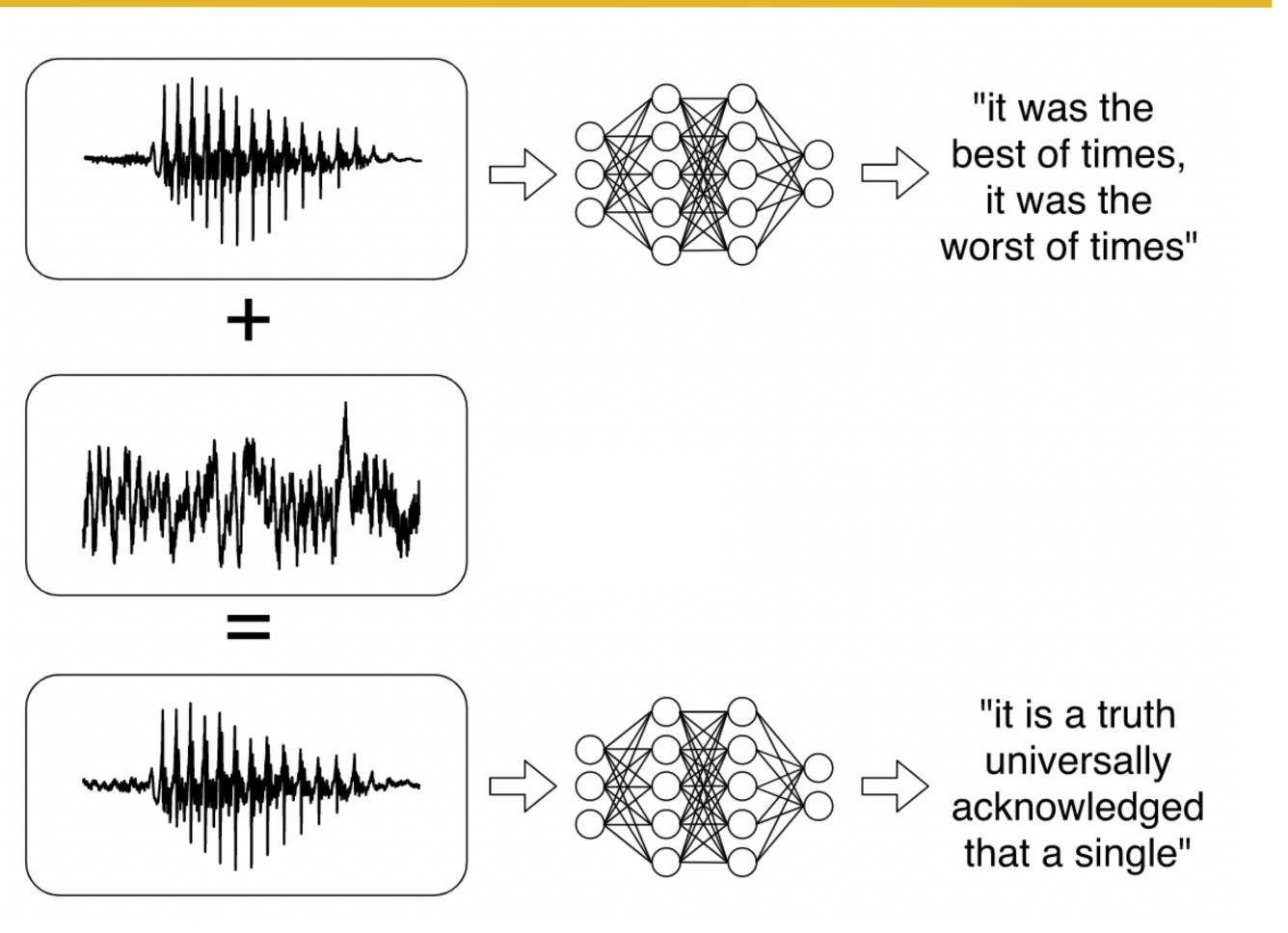






Non-suspicious: The attacker can produce any input example they wish, as long as it would appear to a human to be a real input.

Example: *voice-assistant* attack: unlocking a security system or making an unauthorized purchase, via audio that appears to be harmless or inoffensive, such as a voicemail or television advertisement.





Content-constrained: The attacker can produce any input example they wish, as long as it contains some content payload.

Example: Email spams.





order to induce desired behavior from the machine learning system.

Example: Unlocking a stolen phone by tricking fingerprint/facerecognition system

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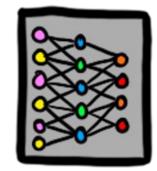
Unconstrained: The attacker can produce any input they want in



settings:

White-box \rightarrow Model is known



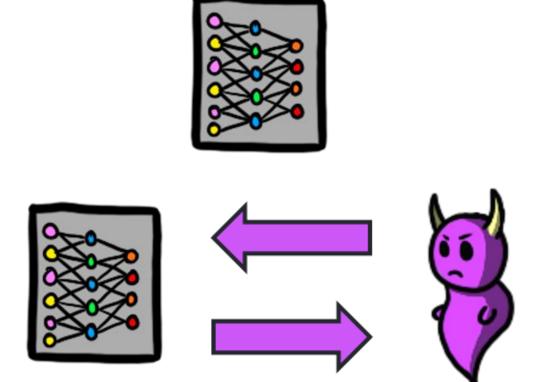




settings:

- White-box \rightarrow Model is known
- Black-box \rightarrow Query access to the model







settings:

- White-box \rightarrow Model is known
- Black-box \rightarrow Query access to the model
- Transferable \rightarrow No query access



settings:

- White-box \rightarrow Model is known
- Black-box \rightarrow Query access to the model
- Transferable \rightarrow No query access
- Gray-box \rightarrow The rest



Adversarial Examples - Defenses

Similarly to many ML-related problems, there is no existing defense that can fully prevent adversarial examples.

What properties do we want from a defense?

- It preserves <u>clean input accuracy</u>. It <u>correctly classifies</u> adversarial examples



Adversarial Examples - Defenses

Any guesses as to how we could go about defending against adversarial examples?

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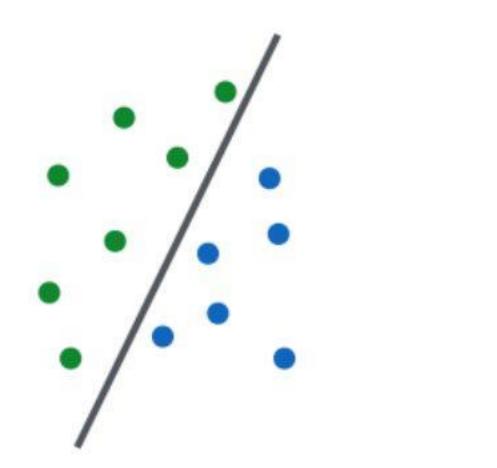
Basic Defense - Adversarial Training

Adversarial Training is a simple defense that goes as follows:

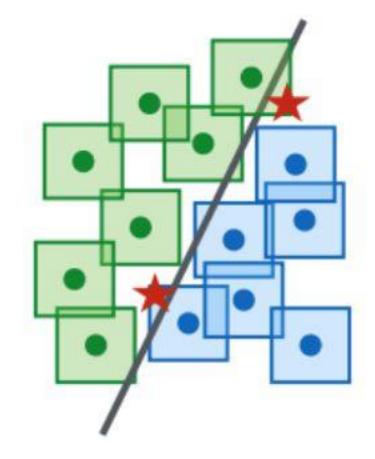
- For a batch D_i of input samples D_i = { $(x_1, y_1), (x_2, y_2), \dots, (x_h, y_h)$ }, b is the batch size.
- Generate adversarial examples D'_i $= \{(x'_1, y_1), (x'_2, y_2), \dots, (x'_h, y_h)\}$
- Train your model on $\overline{D_i} = D_i \cup D'_i$



Basic Defense - Adversarial Training



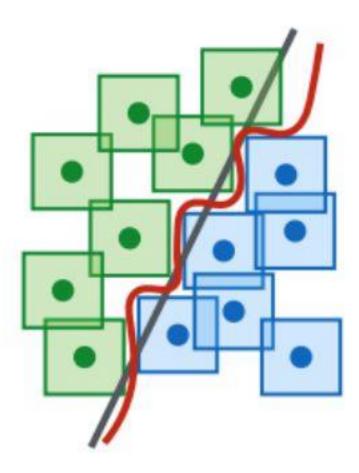
(a) Linearly Separable Samples



Augmenting Training Data with Adversarial Examples

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(b) Samples Augmented with Adversarial Examples



(c) Complex Decision Boundary



Basic Defense - Adversarial Training

Adversarial Training is simple, but effective. It is currently considered one of if not the best existing defense against adversarial examples by the research community.



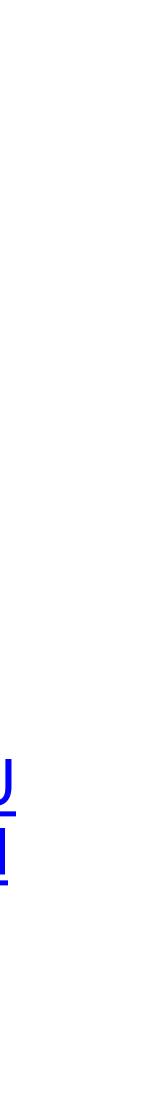


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